

(c) $4^{3/2} = \sqrt{4^3} = \sqrt{64} = 8$ Alternative solution: $4^{3/2} = (\sqrt{4})^3 = 2^3 = 8$

(d) $\frac{1}{\sqrt[3]{x^4}} = \frac{1}{x^{4/3}} = x^{-4/3}$

(e) $\left(\frac{x}{y}\right)^3 \left(\frac{y^2x}{z}\right)^4 = \frac{x^3}{y^3} \cdot \frac{y^8x^4}{z^4} = x^7y^5z^{-4}$



Exercises

A [Click here for answers](#)

1-16 ■ Expand and simplify.

- | | |
|--|-----------------------|
| 1. $(-6ab)(0.5ac)$ | 2. $-(2x^2y)(-xy^4)$ |
| 3. $2x(x - 5)$ | 4. $(4 - 3x)x$ |
| 5. $-2(4 - 3a)$ | 6. $8 - (4 + x)$ |
| 7. $4(x^2 - x + 2) - 5(x^2 - 2x + 1)$ | |
| 8. $5(3t - 4) - (t^2 + 2) - 2t(t - 3)$ | |
| 9. $(4x - 1)(3x + 7)$ | 10. $x(x - 1)(x + 2)$ |
| 11. $(2x - 1)^2$ | 12. $(2 + 3x)^2$ |
| 13. $y^4(6 - y)(5 + y)$ | |
| 14. $(t - 5)^2 - 2(t + 3)(8t - 1)$ | |
| 15. $(1 + 2x)(x^2 - 3x + 1)$ | 16. $(1 + x - x^2)^2$ |

17-28 ■ Perform the indicated operations and simplify.

- | | |
|--|--|
| 17. $\frac{2 + 8x}{2}$ | 18. $\frac{9b - 6}{3b}$ |
| 19. $\frac{1}{x + 5} + \frac{2}{x - 3}$ | 20. $\frac{1}{x + 1} + \frac{1}{x - 1}$ |
| 21. $u + 1 + \frac{u}{u + 1}$ | 22. $\frac{2}{a^2} - \frac{3}{ab} + \frac{4}{b^2}$ |
| 23. $\frac{x/y}{z}$ | 24. $\frac{x}{y/z}$ |
| 25. $\left(\frac{-2r}{s}\right)\left(\frac{s^2}{-6t}\right)$ | 26. $\frac{a}{bc} \div \frac{b}{ac}$ |

27. $\frac{1 + \frac{1}{c-1}}{1 - \frac{1}{c-1}}$

28. $1 + \frac{1}{1 + \frac{1}{1+x}}$

29-48 ■ Factor the expression.

- | | |
|----------------------------|-----------------------------|
| 29. $2x + 12x^3$ | 30. $5ab - 8abc$ |
| 31. $x^2 + 7x + 6$ | 32. $x^2 - x - 6$ |
| 33. $x^2 - 2x - 8$ | 34. $2x^2 + 7x - 4$ |
| 35. $9x^2 - 36$ | 36. $8x^2 + 10x + 3$ |
| 37. $6x^2 - 5x - 6$ | 38. $x^2 + 10x + 25$ |
| 39. $t^3 + 1$ | 40. $4t^2 - 9s^2$ |
| 41. $4t^2 - 12t + 9$ | 42. $x^3 - 27$ |
| 43. $x^3 + 2x^2 + x$ | 44. $x^3 - 4x^2 + 5x - 2$ |
| 45. $x^3 + 3x^2 - x - 3$ | 46. $x^3 - 2x^2 - 23x + 60$ |
| 47. $x^3 + 5x^2 - 2x - 24$ | 48. $x^3 - 3x^2 - 4x + 12$ |

49-54 ■ Simplify the expression.

- | | |
|---|--|
| 49. $\frac{x^2 + x - 2}{x^2 - 3x + 2}$ | 50. $\frac{2x^2 - 3x - 2}{x^2 - 4}$ |
| 51. $\frac{x^2 - 1}{x^2 - 9x + 8}$ | 52. $\frac{x^3 + 5x^2 + 6x}{x^2 - x - 12}$ |
| 53. $\frac{1}{x + 3} + \frac{1}{x^2 - 9}$ | |

54. $\frac{x}{x^2 + x - 2} - \frac{2}{x^2 - 5x + 4}$

55-60 ■ Complete the square.

55. $x^2 + 2x + 5$ 56. $x^2 - 16x + 80$

57. $x^2 - 5x + 10$ 58. $x^2 + 3x + 1$

59. $4x^2 + 4x - 2$ 60. $3x^2 - 24x + 50$

61-68 ■ Solve the equation.

61. $x^2 + 9x - 10 = 0$ 62. $x^2 - 2x - 8 = 0$

63. $x^2 + 9x - 1 = 0$ 64. $x^2 - 2x - 7 = 0$

65. $3x^2 + 5x + 1 = 0$ 66. $2x^2 + 7x + 2 = 0$

67. $x^3 - 2x + 1 = 0$ 68. $x^3 + 3x^2 + x - 1 = 0$

69-72 ■ Which of the quadratics are irreducible?

69. $2x^2 + 3x + 4$ 70. $2x^2 + 9x + 4$

71. $3x^2 + x - 6$ 72. $x^2 + 3x + 6$

73-76 ■ Use the Binomial Theorem to expand the expression.

73. $(a + b)^6$ 74. $(a + b)^7$

75. $(x^2 - 1)^4$ 76. $(3 + x^2)^5$

77-82 ■ Simplify the radicals.

77. $\sqrt{32}\sqrt{2}$ 78. $\frac{\sqrt[3]{-2}}{\sqrt[3]{54}}$ 79. $\frac{\sqrt[4]{32x^4}}{\sqrt[4]{2}}$

80. $\sqrt{xy}\sqrt{x^3y}$ 81. $\sqrt{16a^4b^3}$ 82. $\frac{\sqrt[5]{96a^6}}{\sqrt[5]{3a}}$

83-100 ■ Use the Laws of Exponents to rewrite and simplify the expression.

83. $3^{10} \times 9^8$ 84. $2^{16} \times 4^{10} \times 16^6$

85. $\frac{x^9(2x)^4}{x^3}$

87. $\frac{a^{-3}b^4}{a^{-5}b^5}$

89. $3^{-1/2}$

91. $125^{2/3}$

93. $(2x^2y^4)^{3/2}$

95. $\sqrt[5]{y^6}$

97. $\frac{1}{(\sqrt{t})^5}$

99. $\sqrt[4]{\frac{t^{1/2}\sqrt{st}}{s^{2/3}}}$

86. $\frac{a^n \times a^{2n+1}}{a^{n-2}}$

88. $\frac{x^{-1} + y^{-1}}{(x + y)^{-1}}$

90. $96^{1/5}$

92. $64^{-4/3}$

94. $(x^{-5}y^3z^{10})^{-3/5}$

96. $(\sqrt[4]{a})^3$

98. $\frac{\sqrt{x^5}}{\sqrt[4]{x^3}}$

100. $\sqrt[4]{r^{2n+1}} \times \sqrt[4]{r^{-1}}$

101-108 ■ Rationalize the expression.

101. $\frac{\sqrt{x} - 3}{x - 9}$

102. $\frac{(1/\sqrt{x}) - 1}{x - 1}$

103. $\frac{x\sqrt{x} - 8}{x - 4}$

104. $\frac{\sqrt{2+h} + \sqrt{2-h}}{h}$

105. $\frac{2}{3 - \sqrt{5}}$

106. $\frac{1}{\sqrt{x} - \sqrt{y}}$

107. $\sqrt{x^2 + 3x + 4} - x$

108. $\sqrt{x^2 + x} - \sqrt{x^2 - x}$

109-116 ■ State whether or not the equation is true for all values of the variable.

109. $\sqrt{x^2} = x$

110. $\sqrt{x^2 + 4} = |x| + 2$

111. $\frac{16 + a}{16} = 1 + \frac{a}{16}$

112. $\frac{1}{x^{-1} + y^{-1}} = x + y$

113. $\frac{x}{x + y} = \frac{1}{1 + y}$

114. $\frac{2}{4 + x} = \frac{1}{2} + \frac{2}{x}$

115. $(x^3)^4 = x^7$

116. $6 - 4(x + a) = 6 - 4x - 4a$



Answers

1. $-3a^2bc$ 2. $2x^3y^5$ 3. $2x^2 - 10x$ 4. $4x - 3x^2$
 5. $-8 + 6a$ 6. $4 - x$ 7. $-x^2 + 6x + 3$
 8. $-3t^2 + 21t - 22$ 9. $12x^2 + 25x - 7$
 10. $x^3 + x^2 - 2x$ 11. $4x^2 - 4x + 1$
 12. $9x^2 + 12x + 4$ 13. $30y^4 + y^5 - y^6$
 14. $-15t^2 - 56t + 31$ 15. $2x^3 - 5x^2 - x + 1$
 16. $x^4 - 2x^3 - x^2 + 2x + 1$ 17. $1 + 4x$ 18. $3 - 2/b$
 19. $\frac{3x + 7}{x^2 + 2x - 15}$ 20. $\frac{2x}{x^2 - 1}$ 21. $\frac{u^2 + 3u + 1}{u + 1}$
 22. $\frac{2b^2 - 3ab + 4a^2}{a^2b^2}$ 23. $\frac{x}{yz}$ 24. $\frac{zx}{y}$ 25. $\frac{rs}{3t}$
 26. $\frac{a^2}{b^2}$ 27. $\frac{c}{c - 2}$ 28. $\frac{3 + 2x}{2 + x}$ 29. $2x(1 + 6x^2)$
 30. $ab(5 - 8c)$ 31. $(x + 6)(x + 1)$ 32. $(x - 3)(x + 2)$
 33. $(x - 4)(x + 2)$ 34. $(2x - 1)(x + 4)$
 35. $9(x - 2)(x + 2)$ 36. $(4x + 3)(2x + 1)$
 37. $(3x + 2)(2x - 3)$ 38. $(x + 5)^2$
 39. $(t + 1)(t^2 - t + 1)$ 40. $(2t - 3s)(2t + 3s)$
 41. $(2t - 3)^2$ 42. $(x - 3)(x^2 + 3x + 9)$
 43. $x(x + 1)^2$ 44. $(x - 1)^2(x - 2)$
 45. $(x - 1)(x + 1)(x + 3)$ 46. $(x - 3)(x + 5)(x - 4)$
 47. $(x - 2)(x + 3)(x + 4)$ 48. $(x - 2)(x - 3)(x + 2)$
 49. $\frac{x + 2}{x - 2}$ 50. $\frac{2x + 1}{x + 2}$ 51. $\frac{x + 1}{x - 8}$ 52. $\frac{x(x + 2)}{x - 4}$
 53. $\frac{x - 2}{x^2 - 9}$ 54. $\frac{x^2 - 6x - 4}{(x - 1)(x + 2)(x - 4)}$
 55. $(x + 1)^2 + 4$ 56. $(x - 8)^2 + 16$ 57. $(x - \frac{5}{2})^2 + \frac{15}{4}$
 58. $(x + \frac{3}{2})^2 - \frac{5}{4}$ 59. $(2x + 1)^2 - 3$
 60. $3(x - 4)^2 + 2$ 61. $1, -10$ 62. $-2, 4$
 63. $\frac{-9 \pm \sqrt{85}}{2}$ 64. $1 \pm 2\sqrt{2}$ 65. $\frac{-5 \pm \sqrt{13}}{6}$
 66. $\frac{-7 \pm \sqrt{33}}{4}$ 67. $1, \frac{-1 \pm \sqrt{5}}{2}$ 68. $-1, -1 \pm \sqrt{2}$
 69. Irreducible 70. Not irreducible
 71. Not irreducible (two real roots) 72. Irreducible
 73. $a^6 + 6a^5b + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6ab^5 + b^6$
 74. $a^7 + 7a^6b + 21a^5b^2 + 35a^4b^3 + 35a^3b^4 + 21a^2b^5 + 7ab^6 + b^7$
 75. $x^8 - 4x^6 + 6x^4 - 4x^2 + 1$
 76. $243 + 405x^2 + 270x^4 + 90x^6 + 15x^8 + x^{10}$
 77. 8 78. $-\frac{1}{3}$ 79. $2|x|$ 80. $x^2|y|$
 81. $4a^2b\sqrt{b}$ 82. $2a$ 83. 3^{26} 84. 2^{60} 85. $16x^{10}$
 86. a^{2n+3} 87. $\frac{a^2}{b}$ 88. $\frac{(x + y)^2}{xy}$ 89. $\frac{1}{\sqrt{3}}$
 90. $2^5\sqrt{3}$ 91. 25 92. $\frac{1}{256}$ 93. $2\sqrt{2}|x|^3y^6$
 94. $\frac{x^3}{y^{9/5}z^6}$ 95. $y^{6/5}$ 96. $a^{3/4}$ 97. $t^{-5/2}$ 98. $\frac{1}{x^{1/8}}$
 99. $\frac{t^{1/4}}{s^{1/24}}$ 100. $r^{n/2}$ 101. $\frac{1}{\sqrt{x} + 3}$ 102. $\frac{-1}{\sqrt{x} + x}$
 103. $\frac{x^2 + 4x + 16}{x\sqrt{x} + 8}$ 104. $\frac{2}{\sqrt{2 + h} - \sqrt{2 - h}}$
 105. $\frac{3 + \sqrt{5}}{2}$ 106. $\frac{\sqrt{x} + \sqrt{y}}{x - y}$
 107. $\frac{3x + 4}{\sqrt{x^2 + 3x + 4} + x}$ 108. $\frac{2x}{\sqrt{x^2 + x} + \sqrt{x^2 - x}}$
 109. False 110. False 111. True 112. False
 113. False 114. False 115. False 116. True